

Sunday, February 12

Written Test 1 Review

F

Consider the following check (where 's' is a state of some model 'M', and 'phi' is a syntactically-correct LTL formula):
state $s \models \neg \phi$

F

disproving

In order to show that the above model satisfaction relation does not hold, we need to show that for every path π (i.e., a witness) of M, phi does not hold at any state in π .

\forall path

$\pi = S \rightarrow \dots$
path starts with state S \Rightarrow

$\pi \models \neg \phi$

path

$\exists i \cdot i \in \mathbb{N} \wedge i \geq 1 \wedge \pi^i \models \phi$

to disprove this, need a witness path

for the witness path chosen, all states do not satisfy ϕ

Prove vs. Disprove model satisfaction of $G\phi$.

$$\underline{S}, M \models G\phi$$

$$\forall \pi \cdot \pi = S \rightarrow \dots \Rightarrow$$

$$\pi: S \rightarrow \dots \rightarrow \boxed{S_i \rightarrow \dots}$$

$$\boxed{\pi \models G\phi}$$

$$\pi^i \not\models \phi$$

p.g. P
p.g. $\neg\phi$
 π generates

to disprove:
find a witness $\bar{\pi}$ s.t.
 $\bar{\pi} \in N \wedge |\bar{\pi}| \geq 1 \wedge$

$$\boxed{\bar{\pi} \not\models \phi}$$

ϕ may be just a prop. atom, or ϕ can be complicated, including temporal operators.

$$\forall \bar{\pi} \cdot \bar{\pi} \in N \wedge |\bar{\pi}| \geq 1 \Rightarrow \bar{\pi} \not\models \phi$$

to disprove,

give a path $\pi = S_i \rightarrow \dots$

$$P \notin L(S)$$

WTL.

Prove vs. Disprove model, path sat.

you'll only be given options to choose from.

$$\text{e.g. } S_2 \models \neg\phi$$

$$F \boxed{p} \wedge (\boxed{G \boxed{q} \Rightarrow \boxed{U \boxed{r}}})$$

Consequence

is messy!

Operator Precedence

WTL:
stick to letters
of temporal
operators.

Can this be
the LHS of U op?
NO!

→ Unary temporal X, F, G

Binary temporal U, W, R

Unary Prop. \neg

$$F \boxed{p} \wedge (\boxed{G \boxed{q} \Rightarrow \boxed{r \underline{U} \underline{s}}})$$

An operator
with lower
precedence
than \cup

alternatively:

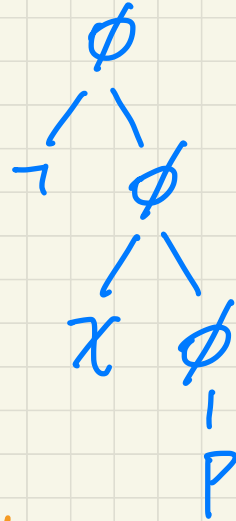
$$\underline{G \underline{q} \Rightarrow r} \cup s$$

not right
 \Rightarrow has lower
precedence
than \cup .

\wedge
 \vee
 \Rightarrow

Assume: questions will not req. a
decision on the associativity of \Rightarrow, X .

$$\underline{\underline{\neg \chi \square}}$$



Q. Consider:

$$P \cup (q \wedge r)$$

$$\Rightarrow \phi \cup \phi$$

$$\Rightarrow P \cup (\phi \wedge \phi)$$

$$\Rightarrow P \cup (\phi \wedge \neg)$$

$$\Rightarrow P \cup (q \wedge r)$$

not LM

- drag and drop trees of derivation steps in correct order

Is this a valid LMD?

parse trees

LM

RMD

make solution available.